

Granular Mechanics and Dusty Plasmas

Christine Hartzell, Daniel Scheeres

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Granular Flows Summer School



University of Colorado **Boulder**



Motivation: Dust

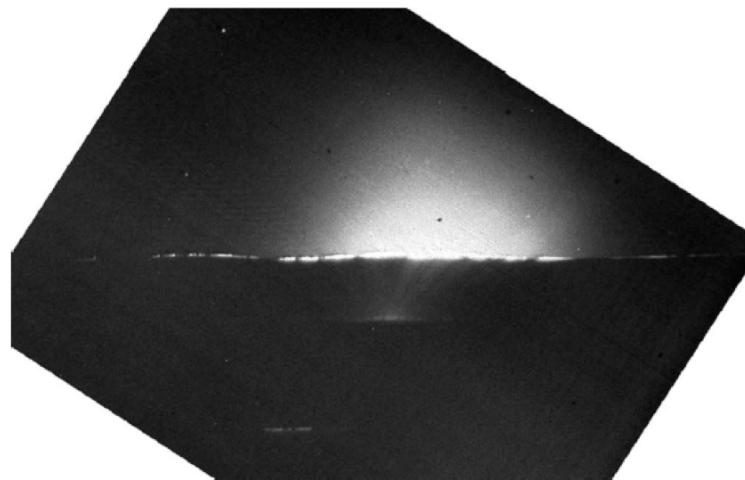


Figure Credit: Colwell et al. *J. Aerospace Engineering* 2009.

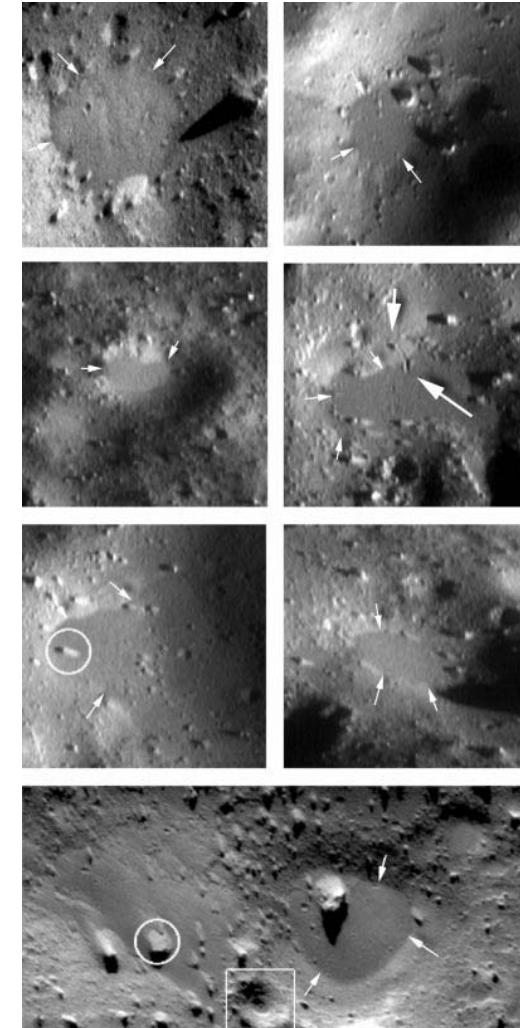
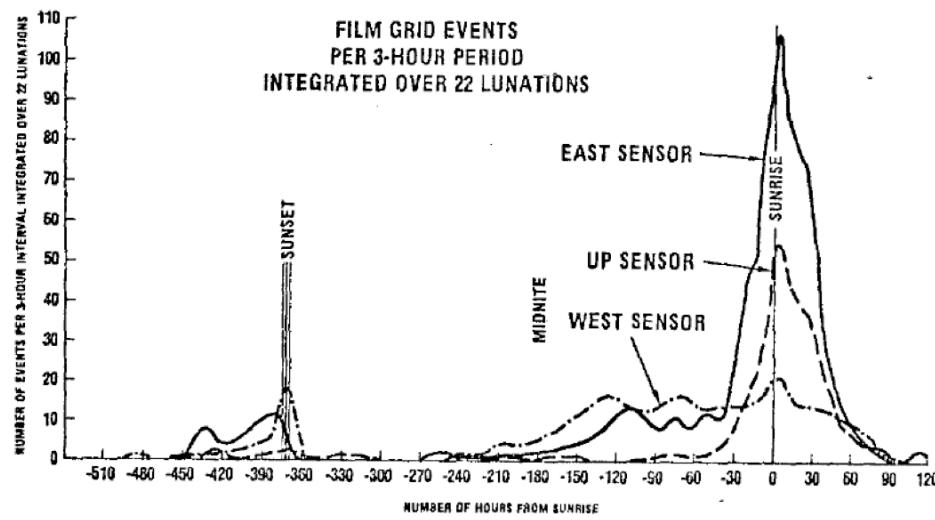
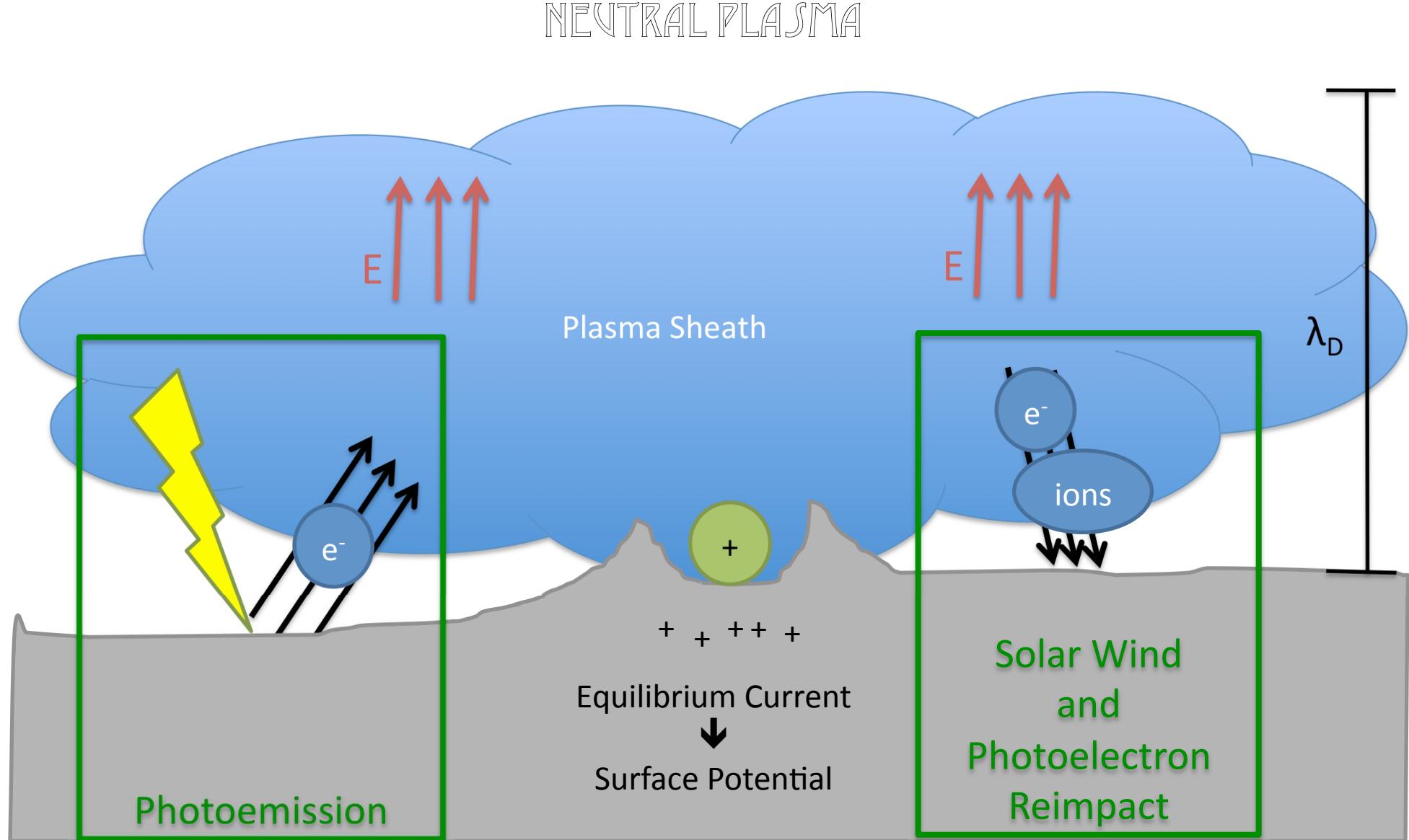


Figure Credit: Berg et al. *Interplanetary Dust and Zodiacal Light* 1976. Figure Credit: Robinson et al. *Nature* 2001.



Intro to Electrostatic Levitation





Outline



- Dust Particle Launching
- Experimental Problems
- Electrostatic Levitation



Equation of Motion



- Model of seismic shaking:

$$\mathbf{a} = A_t \sin(\Omega_t t) \hat{x} + A_n \sin(\Omega_n t) \hat{y}$$

$$a_t = A_t \sin(\Omega_t t)$$

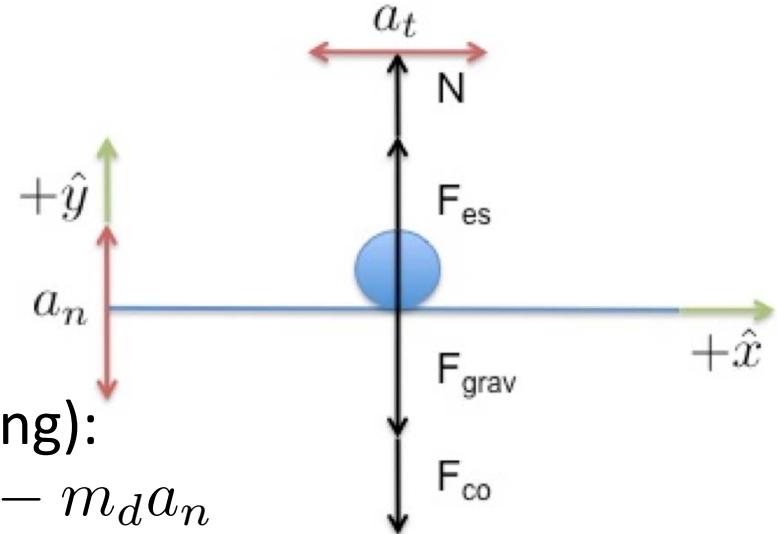
$$a_n = A_n \sin(\Omega_n t)$$

- Equation of Motion (vertical shaking):

$$m_d \ddot{y}_{rel} = F_{es} + F_{grav} + F_{co} + N - m_d a_n$$

- Conditions:

- If $\ddot{y}_{rel} \geq 0$, then the particle is said to be **separated** from the surface. The cohesive force disappears in subsequent motion.
- If $\ddot{y}_i > 0$, the particle is said to be **launched**. The cohesive force disappears in subsequent motion.
- EOM is valid only until particle is no longer in contact with surface (gravity is assumed to be constant).





Force Models



- Gravity: $F_{grav} = -\frac{4}{3}\pi r_d^3 \rho g_s$
- Electrostatic force: $F_{es,gen} = QE$
 - Assume: $Q = EA\epsilon_0$

$$F_{es} = E^2 \pi r_d^2 \epsilon_0$$

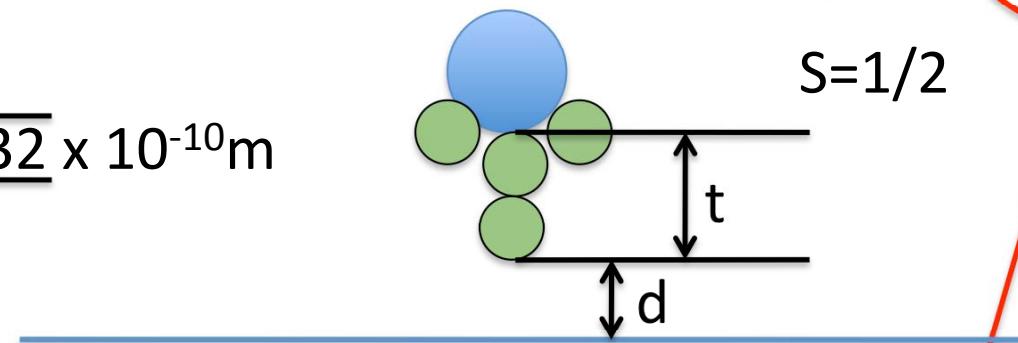


Force Models (Cohesion)



- Cohesion (Perko[23]): $F_{co} = \frac{B}{48(t+d)^2} \frac{r_1 r_2}{r_1 + r_2}$

O⁻² Ion



- Assume:

$$S = 1.32 \times 10^{-10} / t$$

$$B = 4.3 \times 10^{-20} \text{ J}$$

$$F_{co} = -5.14 \times 10^{-2} S^2 r_d$$



Electric Field Required



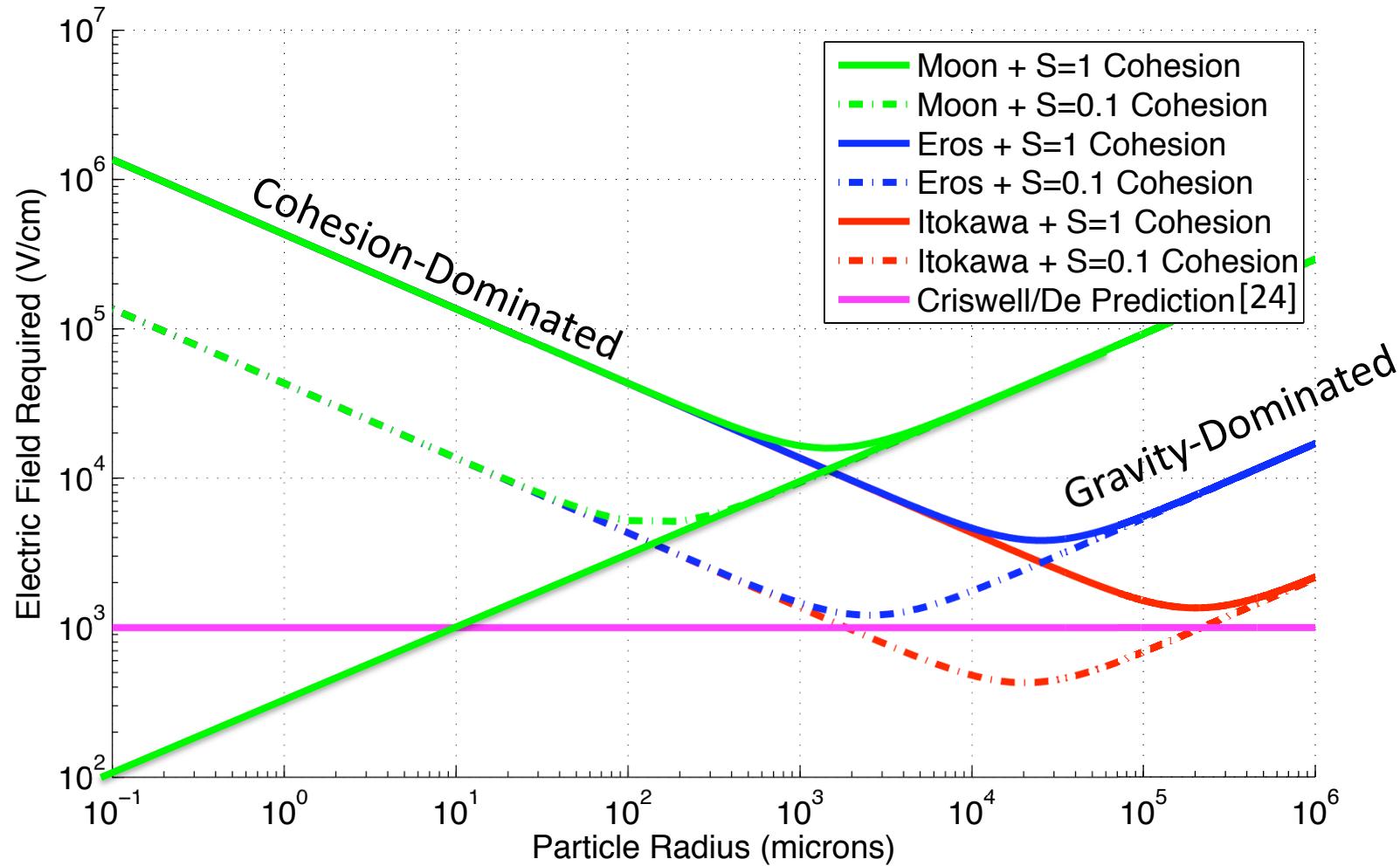
- What electric field strength is required to separate a particle from a surface ($\ddot{y}_{rel} > 0$)?

$$F_{es} \geq m_d a_n - F_{grav} - F_{co}$$

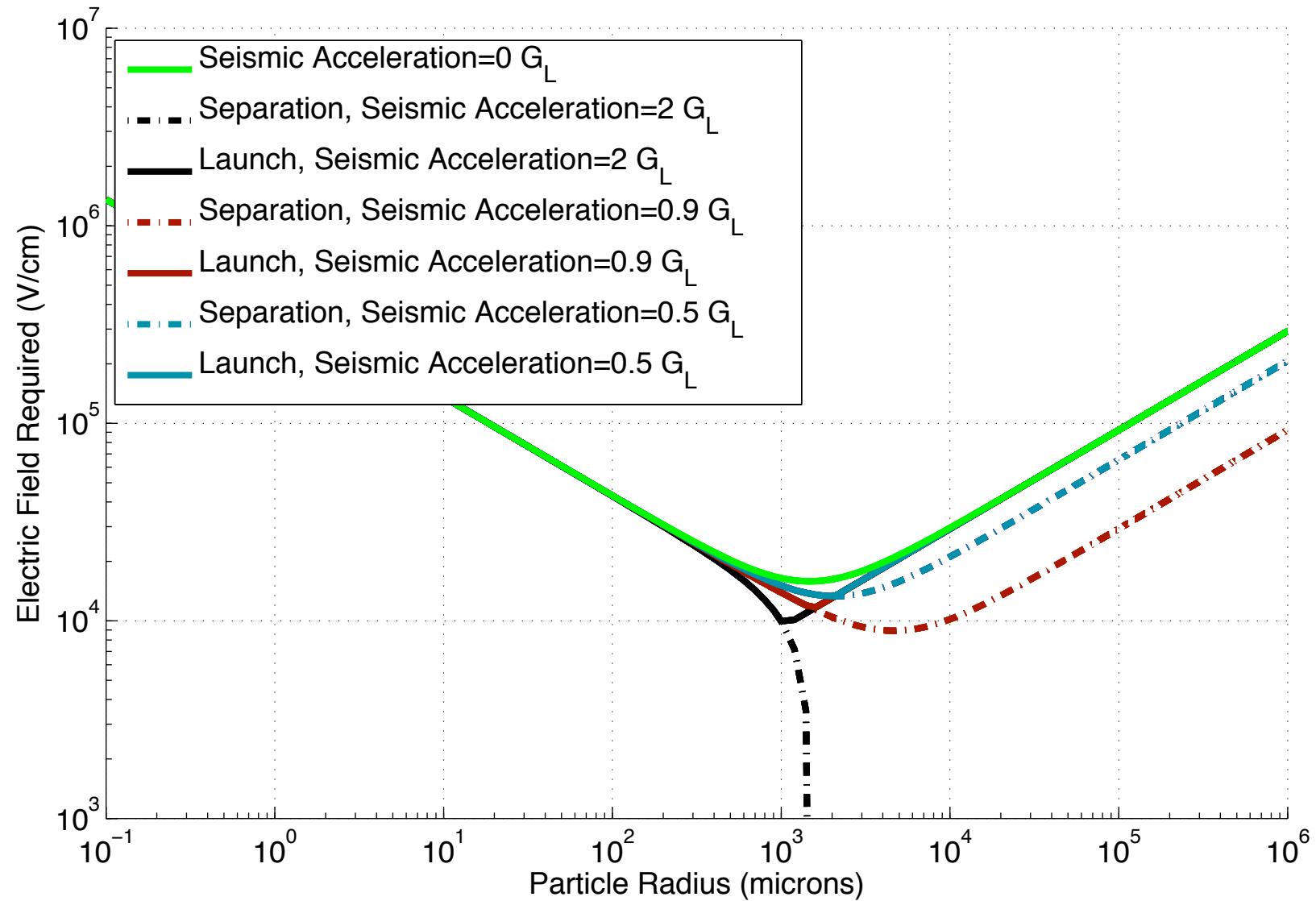
$$E_{req} \geq \left[\frac{4}{3\epsilon_0} r_d \rho (g_s + a_n) + \frac{5.14 \times 10^{-2} S^2}{\pi \epsilon_0 r_d} \right]^{1/2}$$

- If $a_n = 0$, then the electric field is that required to launch a particle.

	Moon	Eros	Itokawa
Gravity	1.622 m/s ²	0.0055 m/s ²	8.603x10 ⁻⁵ m/s ²
Radius	1737.1 x10 ³ m	8420 m	165 m



- $E_{\text{req}} \gg E_{\text{criswell}}$
- Curve minima at large particle sizes (even at S=0.1)
- Curve minima shifted right for asteroids
- See also: Hartzell and Scheeres. *The role of cohesive forces in particle launching on the Moon and asteroids*. Planetary and Space Science.



- Lunar gravity only
- Seismic accelerations do not significantly impact E_{req} for launching



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Experimental Dust Lofting



- Two main dust lofting experiments:
 - Xu Wang et al. 2009, spreading dust mound
 - Flanagan and Goree 2006, dust release from spinning sphere
- With Wang's values $F_{es} < F_{grav}$!!!

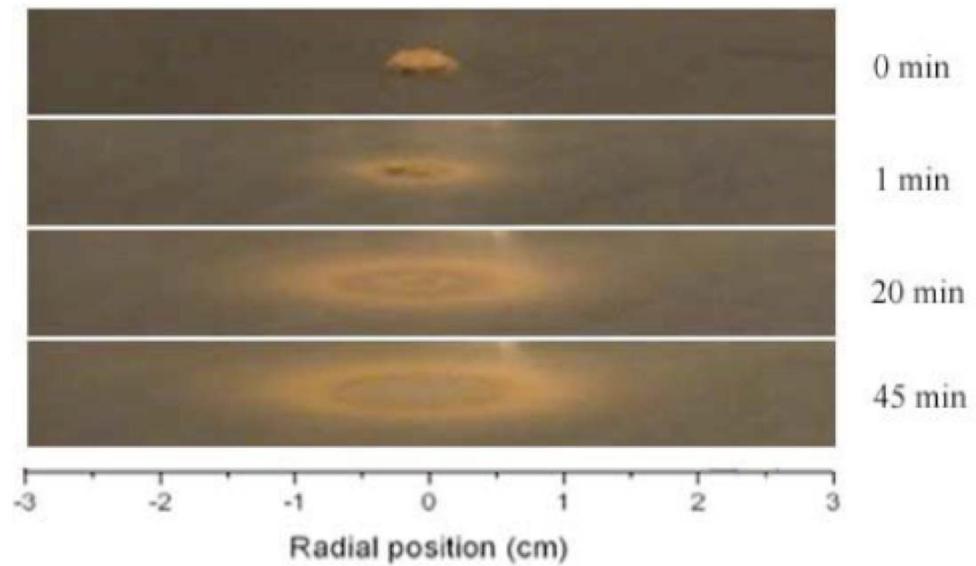


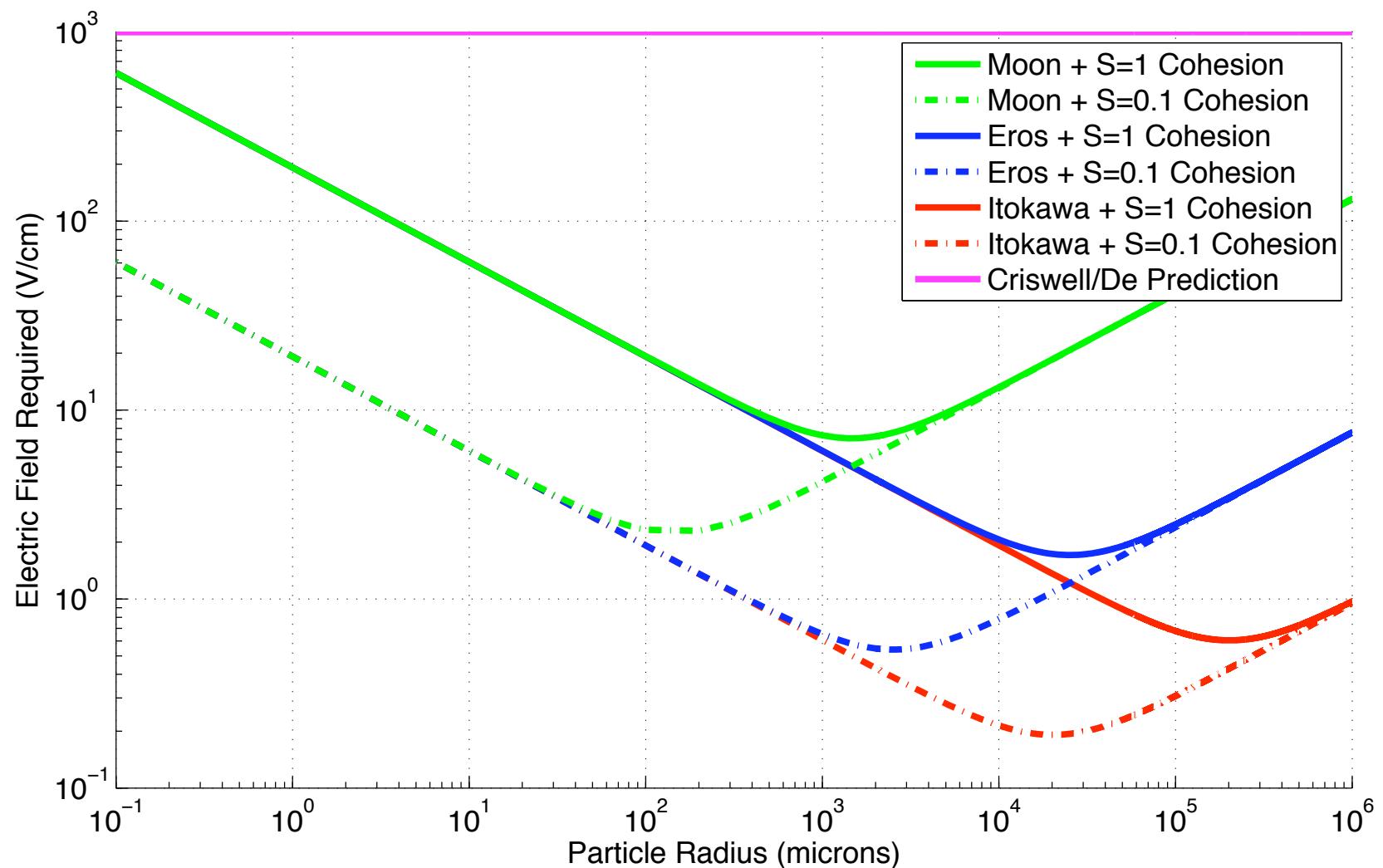
Figure Credit: Wang et al. *JGR* 2009.



Charge Amplification



- We calculate the amount charging level beyond that predicted by Gauss' law that is required to explain experimental results.
- $4.04 \times 10^4 < C_{amp} < 1.04 \times 10^9$
- Use $C_{amp} = 5.01 \times 10^6$
- Can this level of charge amplification occur in reality?



- Lofting possible in terminator
- Still not possible elsewhere (subsolunar = 10^{-1} V/cm)
- Easiest size to loft does not change



Outline



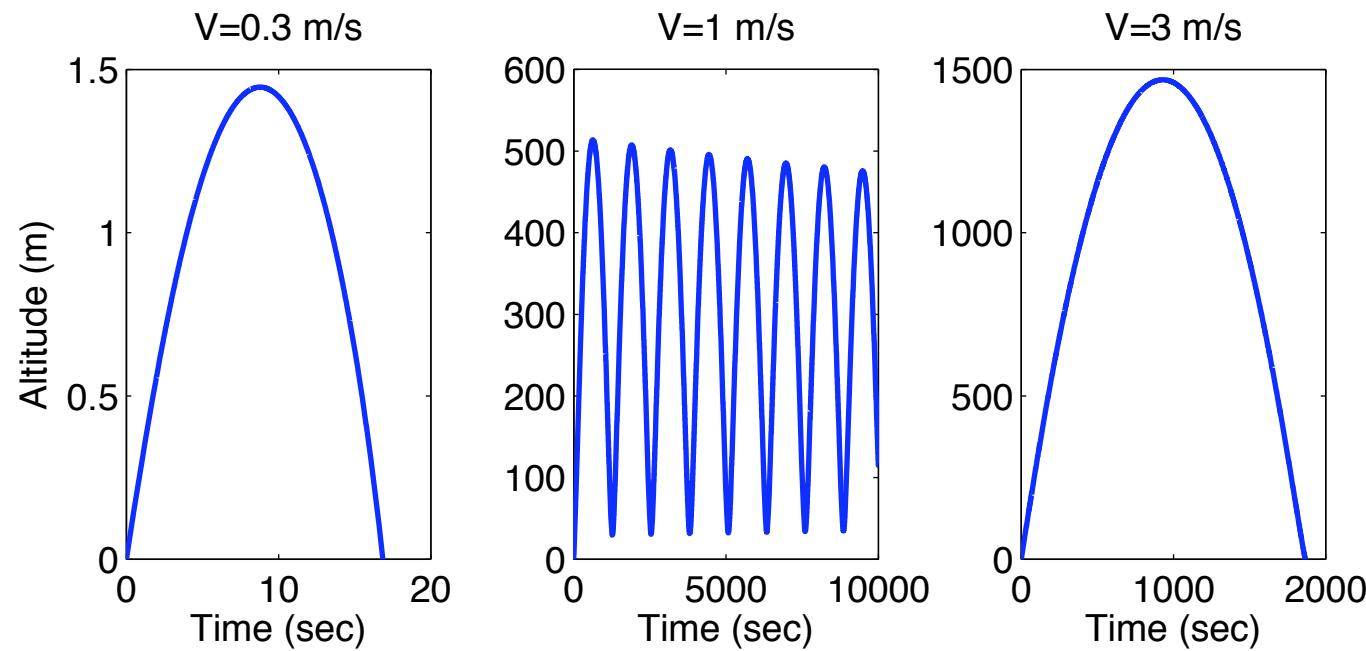
- Dust Particle Launching
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What is Particle Levitation?



- Lacking a feasible launching mechanism, arbitrary initial conditions are chosen.





Plasma Physics Disclaimer



Nitter et al. Model

- Predicts two sheath types
- Non-monotonic sheath has been suggested as more energetically favorable.
- Presence of non-monotonic sheaths supported by PIC models and Lunar Prospector data.

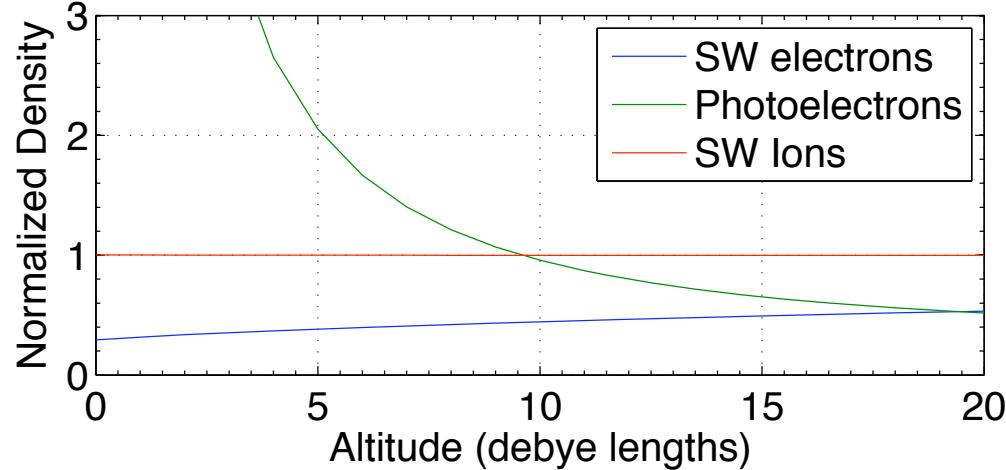
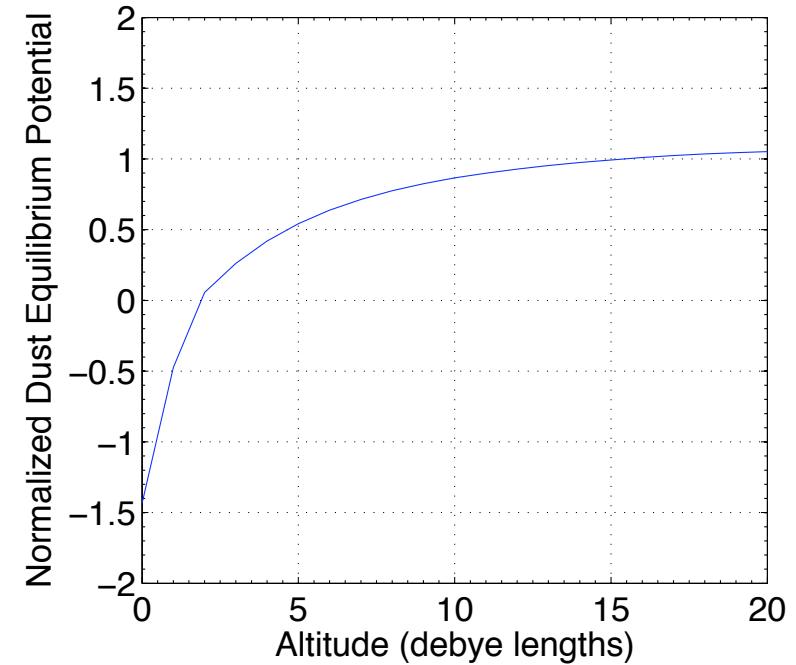
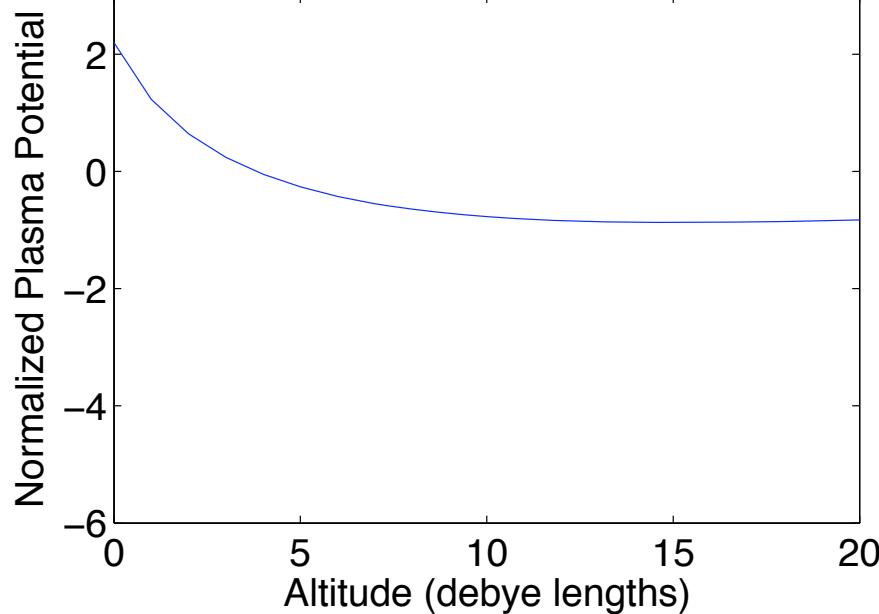
Non-Monotonic Sheath

Colwell et al. Model

- Simpler, analytically-described sheath.
- Only photoelectron density varies with altitude.
- Has been used in previous dust motion studies by Colwell.



Description of Sheath



$$m_d \ddot{h} = qE - \frac{m_d g_s}{\left(\frac{h}{r_c} + 1\right)^2}$$
$$\dot{q} = \sum I(h, q)$$



Linear Stability Analysis



- Define: $F(q, h) = \dot{q}$ $G(q, h) = \ddot{h}$

$$\begin{bmatrix} \delta\dot{q} \\ \delta\dot{h} \\ \delta\ddot{h} \end{bmatrix} = A \begin{bmatrix} \delta q \\ \delta h \\ \delta\dot{h} \end{bmatrix} \quad A = \begin{bmatrix} \frac{\partial F}{\partial q} & \frac{\partial F}{\partial h} & 0 \\ 0 & 0 & 1 \\ \frac{\partial G}{\partial q} & \frac{\partial G}{\partial h} & 0 \end{bmatrix}$$

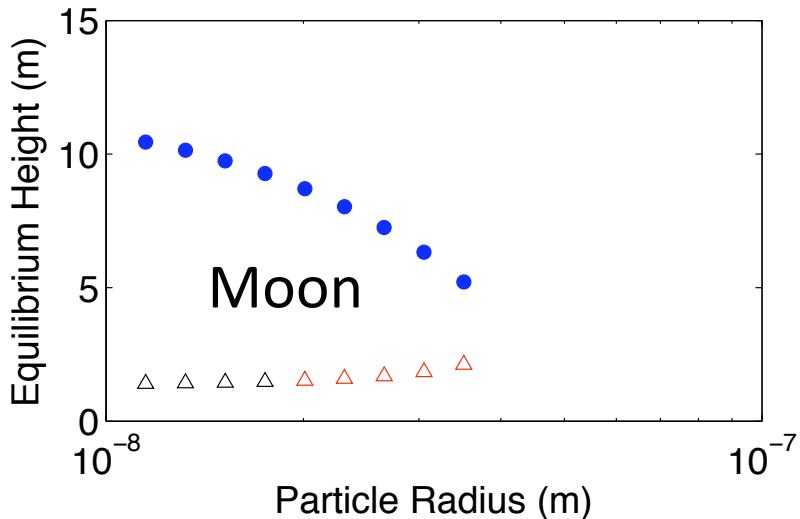
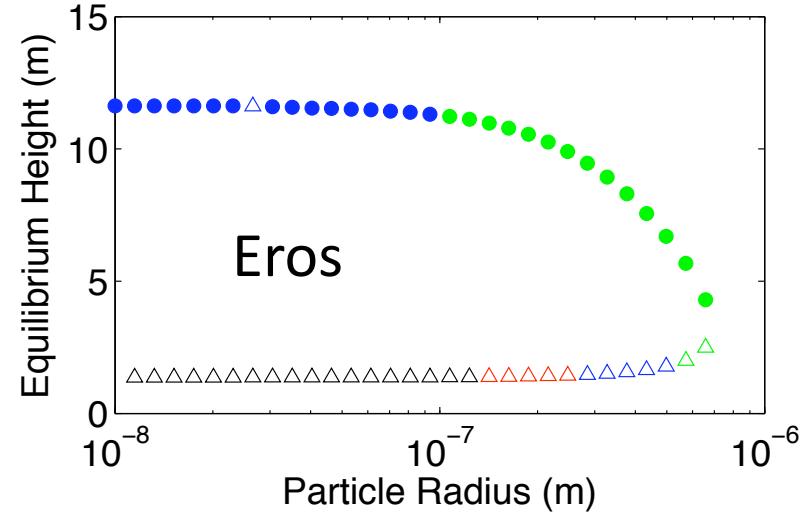
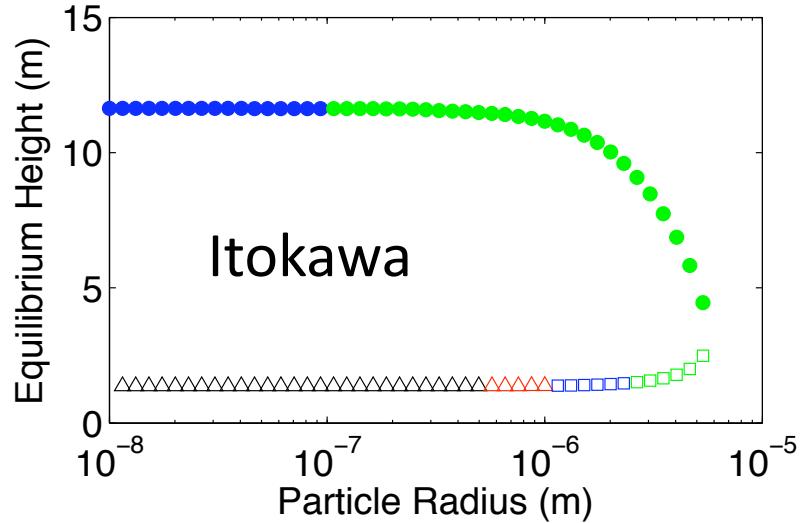
- From A, compute linearized stability by solving for eigenvalues (x):

$$x^3 - F_q x^2 - G_h x + F_q G_h - F_h G_q = 0$$

- Eigenvalues give approximate oscillation frequency and decay constant
- Eigenvectors can be used in nonlinear stability analysis



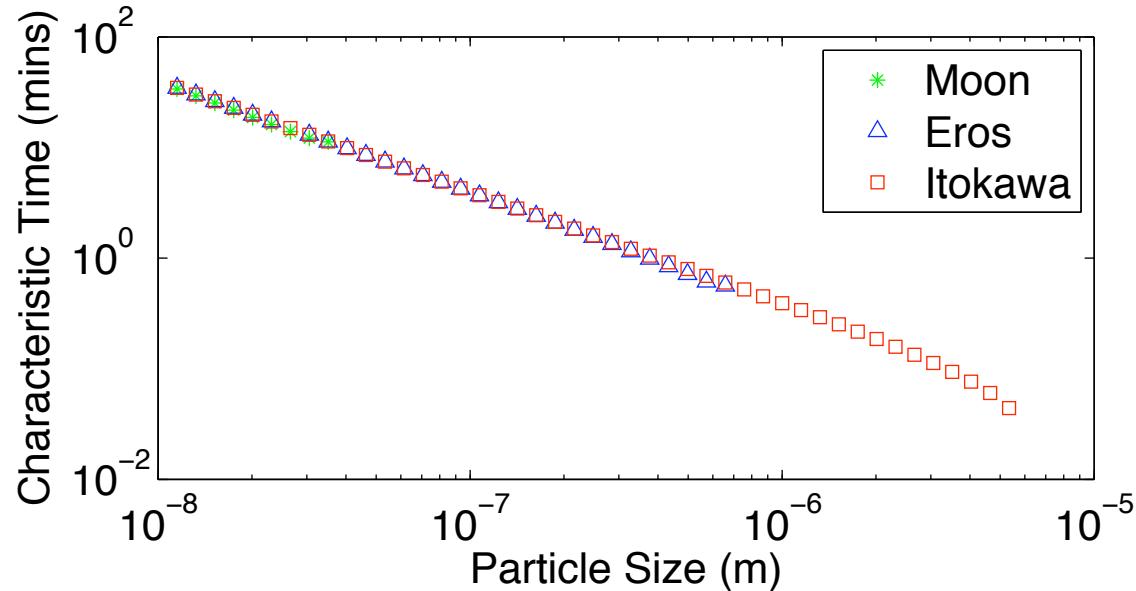
Equilibria



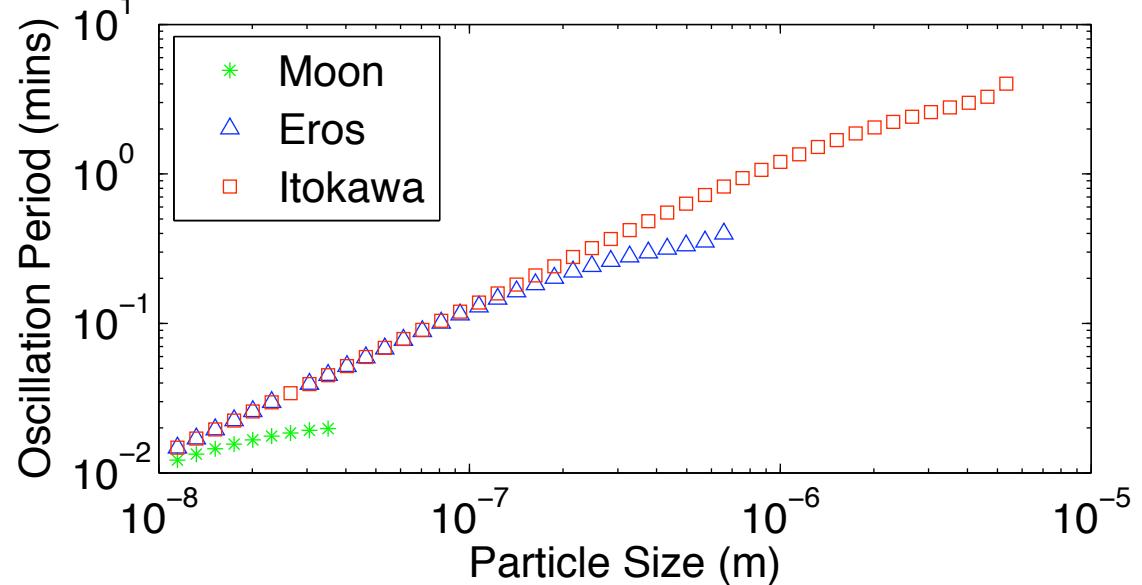
Black: [0,1) electrons
Red: [1, 10) electrons
Blue: [10, 100) electrons
Green: >100 electrons



Timescales of Motion



Rotation Periods:
Itokawa: 12hrs
Eros: 5 hrs
Moon: 27 days

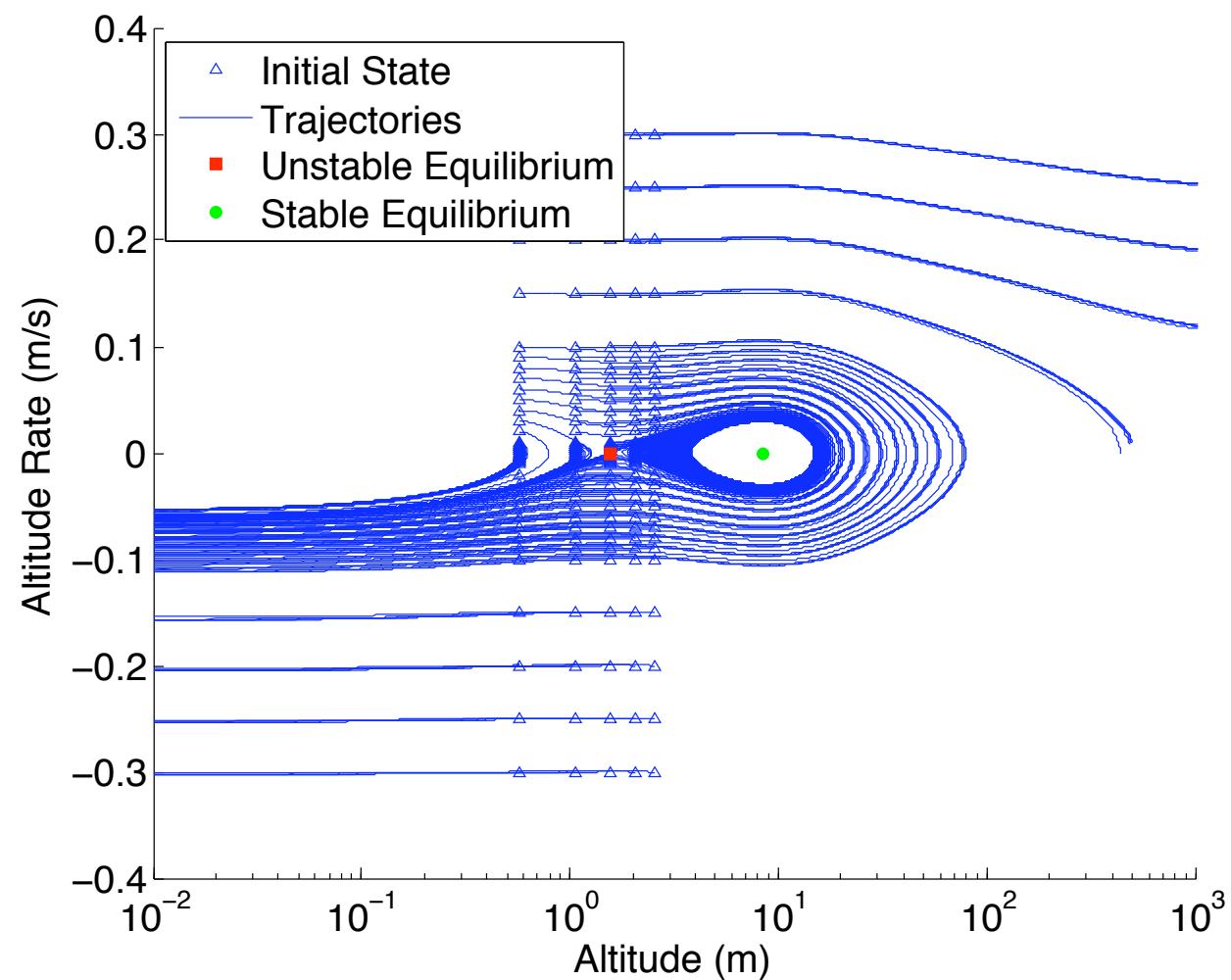




State Space

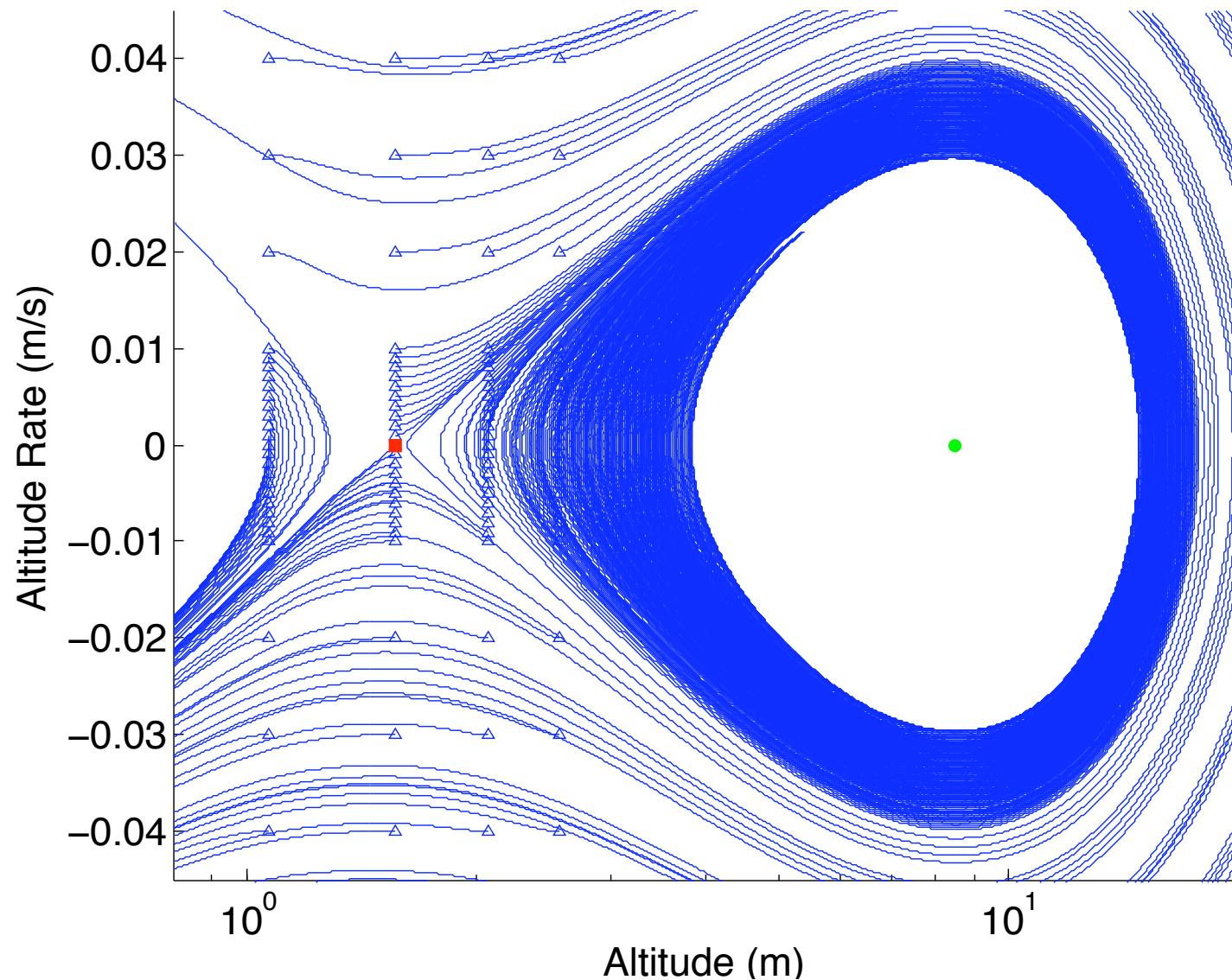


~3micron particle
above Itokawa



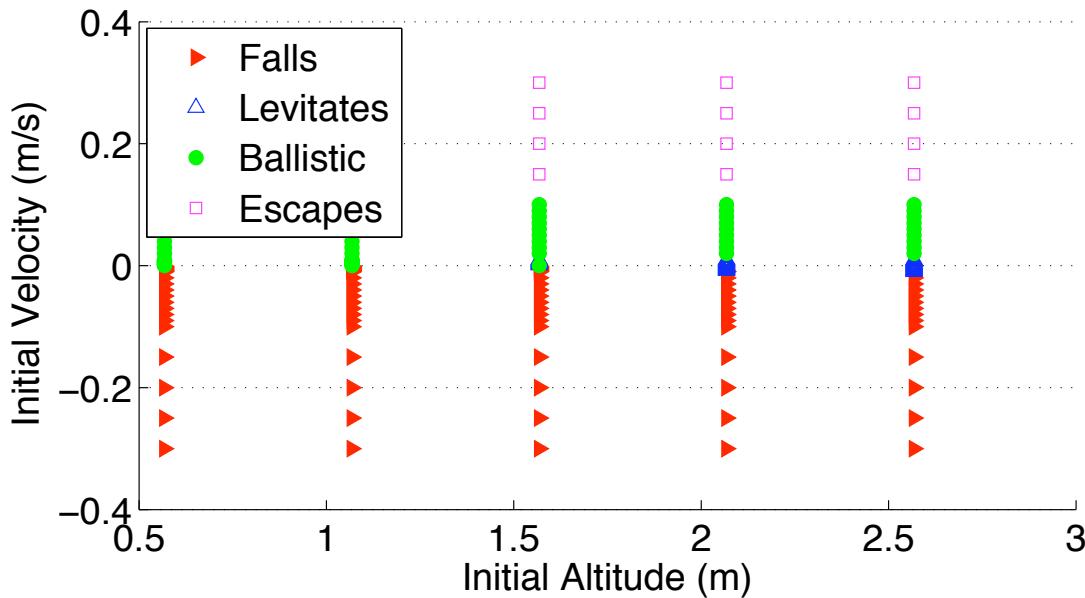


State Space



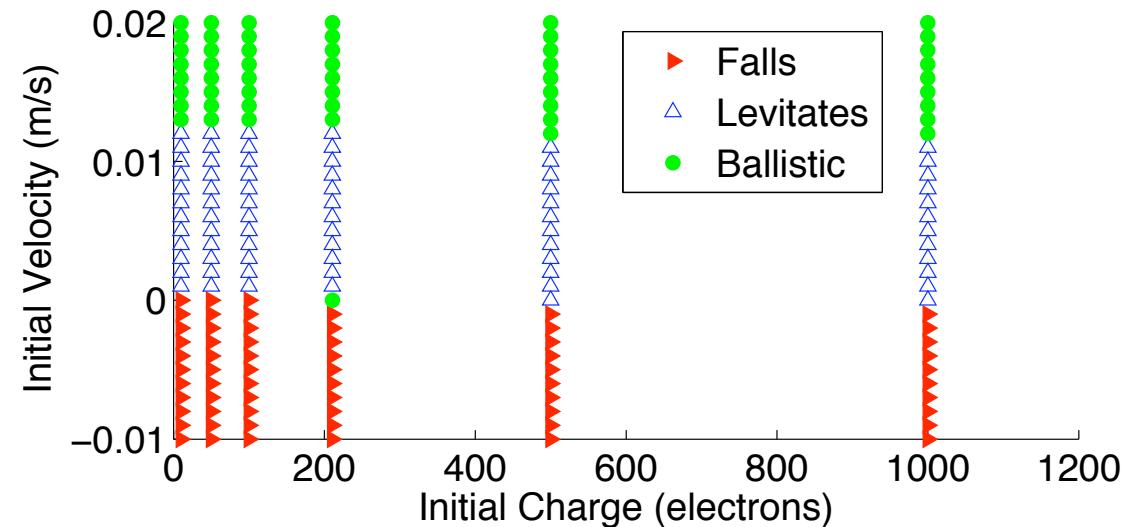


Fate Plots



Initial Charge: 211 e

Initial Altitude: 1.57 m





Conclusions



- Earlier work did not include cohesion when researching electrostatic dust lofting
 - Makes a big difference!
 - Experimental work is also lacking
- Have an increased understanding of levitation after doing dynamical systems analysis
 - Informs which particles will levitate *in situ*
 - Predictions of where to observe levitation



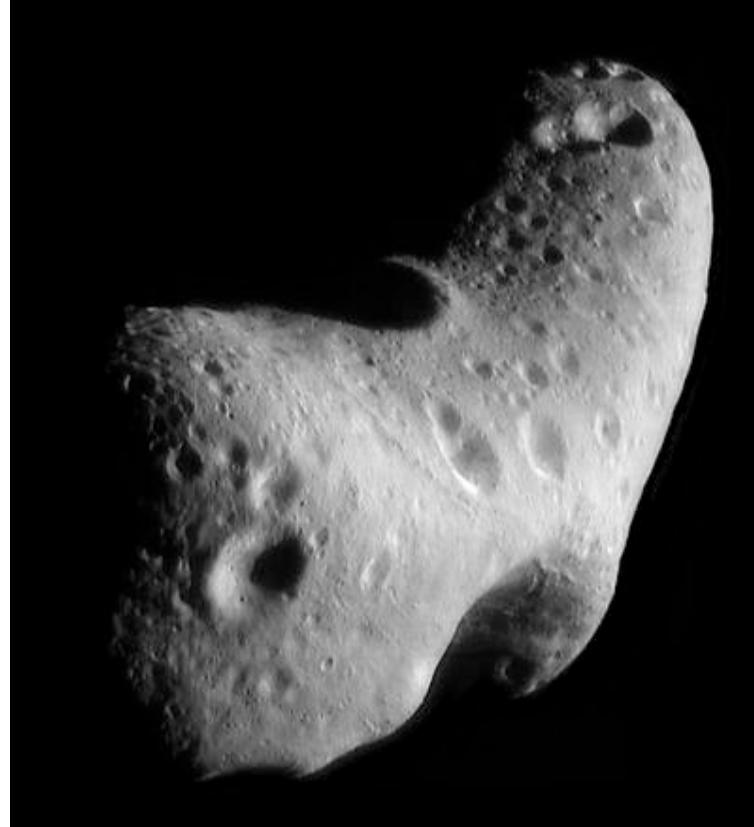
Future Work



- Complete state space exploration for electrostatic levitation
- Model dust motion about 3D asteroid (with accurate gravity)
- Experimental work on cohesion in plasma environment



Questions?



Funding provided by NASA Earth and Space Science Fellowship. Thanks also to my labmates in CSML.